Roll No.							Total No. of Pages

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## B.Tech. (Sem.-1<sup>st</sup>)

# ENGINEERING MATHEMATICS-I

## Subject Code : BTAM-101 (2011 & 2012 Batch)

## Paper ID : [A1101]

Time : 3 Hrs.

Max. Marks : 60

: 03

## **INSTRUCTION TO CANDIDATES :**

- 1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION B & C. have FOUR questions each.
- 3. Attempt any FIVE questions from SECTION B & C carrying EIGHT marks each.
- 4. Select atleast TWO questions from SECTION B & C.

#### **SECTION-A**

1. a) Find asymptotes, parallel to axes, of the curve :

 $x^2 y^2 - xy^2 - x^2y + x + y + 1 = 0.$ 

- b) Write a formula to find the volume of the solid generated by the revolution, about *y*-axis, of the area bounded by the curve x = f(y), the *y*-axis and the abscissae y = a and y = b.
- c) What is the value of  $\frac{\partial(u,v)}{\partial(x,y)} \times \frac{\partial(x,y)}{\partial(u,v)}$ ?
- d) If an error of 1% is made in measuring the length and breadth of a rectangle, what is the percentage error in its area?
- e) Find the equation of the tangent plane to the surface

$$z^2 = 4(1 + x^2 + y^2)$$
 at (2, 2,6).

f) What is the value of 
$$\int_{0}^{1} \int_{x^{2}}^{2-x} xy dx dy$$

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g) Give geometrical interpretation of 
$$\int_{0}^{1} \int_{0}^{1-x} dx dy$$
.

- h) Show that the vector field  $\overrightarrow{F} = (x^2 y^2 + x)\hat{i} (2xy + y)\hat{j}$  is irrotational.
- i) What is the value of  $\nabla \times (xy\hat{i} + yz\hat{j} + zx\hat{k})$ ?
- j) State Stoke's theorem.

#### **SECTION-B**

2. Trace the following curves by giving their salient feature:

a) 
$$x^3 + y^3 = 3axy$$
.

- b)  $r = a(1 + \cos\theta)$  (4,4)
- 3. a) Find the perimeter of the cardioid  $r = a (1-\cos \theta)$ .
  - b) Find the area bounded by two parabolas  $y^2 = 4x$  and  $x^2 = 4y$ . (4,4)

4. a) If 
$$u = \frac{y}{z} + \frac{z}{x}$$
, show that  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z} = 0$ .

b) State Euler's theorem for homogeneous functions and apply it to show that

$$x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} = 3 \tan u$$
  
where  $\sin u = \frac{x^2 y^2}{x + y}$  (4,4)

- 5. a) Find points on the surface  $z^2 = xy + 1$  nearest to the origin.
  - b) Find percentage error in the area of an ellipse if one percent error is made in measuring its major and minor axes. (4,4)

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#### **SECTION-C**

6. a) Evaluate the following integral by changing the order of integration :

$$\int_{0}^{3} \int_{1}^{\sqrt{4-x}} (x+y) \, dx \, dy$$

b) Find the volume of the ellipsoid  $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1.$  (4,4)

7. a) Find a unit vector normal to the surface  $x^3 + y^3 + 3xyz = 3$  at the point (1, 2, -1).

b) If 
$$\overrightarrow{F} = (x + y + 1) \hat{i} + \hat{j} - (x + y)\hat{k}$$
, show that  $\overrightarrow{F}$ . curl  $\overrightarrow{F} = 0$ .

(4, 4)

8. a) Compute the line integral 
$$\int_{C} (y^2 dx - x^2 dy)$$
, where C is the boundary

of the triangle whose vertices are (1,0), (0,1) and (-1, 0).

b) Compute  $\int_{S} \vec{F} \cdot \hat{Nd}s$ , where  $\vec{F} = 6z\hat{i} - 4\hat{j} + y\hat{k}$  and S is the portion

of the plane 2x + 3y + 6z = 12 in the first octant. (4,4)

9. State Gauss Divergence theorem and verify it for

 $\vec{F} = (x^2 - yz)\hat{i} + (y^2 - zx)\hat{j} + (z^2 - xy)\hat{k} \text{ taken over the rectangular}$ parallelopiped  $0 \le x \le a, \ 0 \le y \le b, \ 0 \le z \le c.$  (8)

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